important in limiting the low temperature strength achieved in hot-pressed material. Moreover, the anisotropy of grain shape and the crystallographic preferred orientation, which appear to be related phenomena, have been shown to introduce marked directionality of physical and mechanical properties in hotpressings of  $Si<sub>3</sub>N<sub>4</sub>$  [6]. Further microstructural investigation is required to establish clearly the quantity and distribution of the amorphous constituent.

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## *Electrochemical aspects of dielectric breakdown in alkali harldes*

In metal-insulator-metal sandwiches involving alkali halides, it is found that an application of a suitable voltage (i.e. field) across the sandwich gives rise to the decomposition of the insulator [1 ]. In an alkali halide MX, the reaction at the anode is

$$
X^- + \text{Anode} \rightarrow \frac{1}{2} X_2 + e + \text{Anode} \qquad (1)
$$

where  $X_2$  is the molecular halogen gas. The corresponding cathodic reaction may thus be written as

$$
e_{\text{cathode}} + \square_{\text{insulator}} \rightarrow \square_{\text{insulator}}. (2)
$$

Greene *et al* [1] have noted that for the "forming" (ie. electrolysis) to occur, the forming voltage,  $V_F$ , must just exceed,  $\Delta G$ , the free energy change involved in the overall electrolysis reaction, presumably because

$$
\Delta G = -nFE_0 \tag{3}
$$

where  $E_0$  is the electrode potential (i.e. reversible) of the electrolysis reaction to which *AG*  refers;  $n$  is the number of charge carriers transferred in the overall reaction and  $F$  is the Faraday. For electrolysis to occur,  $V_f$  must

- 
- *\*Notes:* 1. Since alkali halide are uni-univalent, *AG/mole = AGe.*  2. Since alkali halides are solids, entropy would be a rather negligible part of *AGe;* for condensed phases in

general, entropy considerations are relatively unimportant.

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exceed  $E_0$  (and hence  $\Delta G$ ) because some overpotential must be developed before the electrolysis can occur.

This note attempts to correlate the  $V_f$  values of these alkali halides to their band gaps,  $E_g$ values. Also, the relation of these considerations to the experimental values of the dielectric breakdown field for several alkali halides [2] will also be examined.

Since for the solid-state electrolysis to commence, the (exothermic) free energy of formation of the insulator must be just exceeded by the formation voltage [1 ] it follows that

$$
eV_{\rm f} \simeq -\Delta G \tag{4}
$$

where  $V_f$  is the forming voltage of the insulator, e is the electronic charge and  $\Delta G$  is its free energy of formation per mole. For the alkali halides,  $\Delta G$  per *mole* is the same thing as  $\Delta G_e$ , the free energy of formation per *equivalent*  which may also be approximated as the heat of formation per equivalent, *AHe,* so that\*

$$
V_{\mathbf{f}} \simeq -\Delta G \simeq -\Delta G_{\mathbf{e}} \simeq -\Delta H_{\mathbf{e}}. \qquad (5)
$$

Now, it may be noted that [3, 4]

$$
E_{\rm g} \simeq 2(-\Delta H_{\rm e}) \tag{6}
$$

where  $E_{\rm g}$  is the band gap of the compound, the



*Figure 1* A correlation between the forming voltage,  $V_i$ , of the shown alkali halides (placed in a metal-insulatormetal sandwich configuration) versus their band gap,  $E_{\rm g}$ values. See Table I for data and source references.

alkali halide in the present discussion. From Equations 5 and 6 one gets

$$
V_{\mathbf{f}} \simeq \frac{1}{2} E_{\mathbf{g}} \tag{7}
$$

i.e. the forming voltage is half the band gap value. For the insulators where data on both  $V_f$  [1] and  $E_g$  [3, 4] exist, Equation 7 is roughly obeyed (Fig. 1); the data on  $V_f$  and  $E_g$  have also

TABLE I

Compound	$V_{\rm f}$ (eV)	$E_{\rm g}$ (eV)	
CaF <sub>2</sub>	6.2	12	
LiF	$\sim$ 6.1	12	
KCI ×.	4.5	7.6	
<b>KBr</b>	4.1	8.0	
CsI <sup></sup>	3.8	7.0	

*Notes*: 1. The  $V_f$  values are from [1] and the  $E_g$  values from  $[3, 4]$ . It is *not* indicated  $[1]$  that  $V_t$  values refer to single crystals.

> 2. The  $V_f$  values for MgF<sub>2</sub> and MnF<sub>2</sub> are available [1] but no  $E_{\rm g}$  value could be found for them.

been given in Table I together with their source references.

Forming destroys the insulator irreversibly and thus leads to dielectric breakdown; it is of interest, therefore, to compare the forming voltages [1] to,  $(F_{\text{exp}})$ , the experimental values of the dielectric breakdown fields [2] for the alkali halides for which the data are available (Fig. 2). Since  $log(F_{exp})$  increases with increasing  $V_f$  (Fig. 2), increasing log ( $F_{\text{exp}}$ ) should also be





*Figure 2* A plot of  $V_f$  against the experimental values of the dielectric breakdown field,  $F_{\text{exp}}$ , for the shown alkali halides. See Table II for data and source references.

*Figure 3* A plot of  $F_{\text{exp}}$  versus  $E_{g}$  values for the shown alkali halides. See Table II for the data and source references.



*Figure* 4 A plot of  $F_{\text{exp}}$  versus the heat of formation per equivalent (exothermic),  $-\Delta H_e$ , values for the shown alkali halides. See Table II for the data and source references.

associated with increasing  $E_{\rm g}$  values. This is roughly verified on the basis of data in Table II, as plotted in Fig. 3. Equation 6 can also provide a means of relating  $F_{\text{exp}}$  of alkali halides to one of their fundamental thermodynamic parameters, namely, the  $-\Delta H_e$  values. A good correlation is indeed obtained (Fig. 4) with log  $(F_{\rm exp})$  increasing with increasing  $(-\Delta H_e)$  values. The  $-AH_e$  data are listed in Table II and can be taken from any standard compilation, e.g. [5].

It should be stressed here that the line of reasoning developed here as well as the correlations depicted (Figs. 1 to 4) must be recognized as indicating rough correlative trends only and not as a formulation of a rigorous theoretical viewpoint. This is because the arguments presented are based on quasi-thermodynamic concepts derived from data on aqueous electro-





*Notes:* 1. The experimental dielectric breakdown values are from [2] and are *not* claimed to refer to single crystals.

2. The band gap,  $E_g$ , values are from [3, 4].

3. The (exothermic) heat of formation,  $-\Delta H_e$ , values are from [5].

lytes and their application to solids may be somewhat debatable because in solids, the diffusion is slow, the activation energies involved are much greater and, several energy barriers of the same order of magnitude are usually encountered [6].

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